Characterisation of turbulent flow and the wake of a tidal stream turbine in proximity to a ridge

Sulaiman Hurubi, Tim Stallard, Peter K. Stansby, Hannah Mullings and Pablo Ouro

Abstract-Fast tidal currents are generally found in shallow water depths where tidal turbines can be deployed to operate. In complex environments in which there is an irregular bathymetry, seabed shape changes can induce pressure gradients that accelerate or decelerate the flow depending on the slope and relative depth, affecting turbine wake recovery. In this study, a laboratory scale turbine, represented numerically using an Actuator Line Method (ALM), is computed using Large-Eddy Simulations (LES) over a flat-bed and in presence of three short ridges with varying streamwise lengths. Turbines are positioned at several locations, namely at ridge-centre (0D) and at 2Dupstream and downstream from the foot of the ridge to establish the influence of location on wake recovery rate. Turbine operating point is selected to yield a constant tipspeed ratio based on the disc-averaged velocity at each location obtained from a precursor simulation run without turbines. Results show that, relative to the same turbine in a flat channel, there is a noticeable enhancement of the rate of wake recovery when turbine is sited upstream of the ridge and it experiences high fatigue loads when sited downstream of the ridge. Implications for array design regarding performance losses due to turbine- and bathymetry-induced wakes are drawn.

Index Terms—Tidal stream turbine, Bathymetry, Large-eddy simulations, Wake recovery.

I. INTRODUCTION

TIDAL stream power generation has been shown to offer a reliable and consistent source of energy due to its predictable and cyclic nature. However, fast tidal currents are mostly located in shallow water depths locations. In these conditions, the vertical extent of the water column is constrained by the water surface and seabed bathymetry. The interaction between tidal currents and the seabed can result in complex flow patterns, i.e. the generation of coherent flow structures

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[1], that can impact the performance and wake recovery rate of tidal turbines. These effects are important to account for in future multi-row tidal arrays as the spacing between rows could vary between deployment locations within the same site based on the local bathymetry.

Tidal energy sites may exhibit complex bathymetric features with considerable spatial variation in current and turbulence properties [1]. In Ramsey Sound (Pembrokeshire, Wales, UK), Harrold and Ouro [2] show that there is a variation in flow speed during ebb and flood tidal phases at the turbine location, which is partly attributed to the irregular bathymetry found there. The bathymetry map shows that there are ridgelike bed features just over 5 diameters from the turbine location. This sudden change in site bathymetry surrounding the turbine location in Ramsey Sound results in different velocity and turbulence intensity values during a full tidal cycle [3]. Moreover, high energy tidal sites in the Alderney Race (Raz Blanchard in French) are studied by Bourgoin et al. [4], and it was found that large flow structures and high turbulence are generated over rocky plateaus and dune crests.

In a full tidal cycle, tidal turbines located upstream of an obstacle, e.g. ridge or pinnacle, during one tidal phase will develop a wake affected by the bathymetryinduced favorable pressure gradient (FPG) that may accelerate wake recovery, as observed in wind turbines that operate upstream of a hill [5]-[8]. Whereas in the reversed flow direction, the ridge is located upstream of the turbine generating a wake that can affect the turbine's unsteady loading and also the recovery of the turbine's wake. Such effects depend on the relative distance between the device and bed form [6]. These changes in flow conditions can cause the turbines to be exposed to high levels of fatigue loads [9]. Thus, turbine deployment locations need to account for the effect of bathymetry features during the two phases of the tidal cycle, i.e. balancing a faster wake recovery when the obstacle is downstream with loading increase when in the reversed flow.

Until now, the majority of research conducted in tidal stream turbine field has focused on the analysis of uniform flat bed conditions, with little attention given to turbulence induced by variations in bathymetry [1], [10]–[13]. However, it is worth noting that bathymetry-induced turbulence can actually be beneficial in terms of wake recovery rate, as it enhances turbulent transport of momentum [14]–[16]. Considering irregular

terrains, a flow speed-up occurs on hill/ridge tops, which has been reported to be advantageous for wind turbines sited in those locations [17]. However, turbine wake in this location is found to show a slower wake recovery compared to flat terrain, which is attributed to the adverse pressure gradient (APG) present on the downstream side of the ridge slope [5]. Therefore, is important to characterise the effect that steep and elongated ridges can have on tidal turbine wakes in such locations where the APG side of the ridge is far from the FPG side.

In this work, a high-fidelity Large-Eddy Simulation (LES) code is employed to evaluate the wake recovery of a tidal stream turbine operating in proximity to idealised ridges with differing lengths. The aim of this study is to identify how ridge length and turbine location drive the wake recovery behind the turbine when comparing with flat-bed case.

II. NUMERICAL METHODS

To accurately quantify the contribution of ridge-induced pressure and turbulent stresses to the recovery of a tidal turbine's wake, high-fidelity Large-Eddy Simulations (LES) are performed using the Digital Offshore Farm Simulator (DOFAS) [18], an in-house code which has been validated for open channel flows and the flows downstream of tidal stream turbines [10], [19].

DOFAS employs staggered-storage of velocities on Cartesian grids and stores pressure in the cell centre, with full parallelisation using a Message Passing interface (MPI) to ensure computational efficiency. The solver resolves the spatially filtered Navier-Stokes equations for unsteady and incompressible viscous flows. The convection and diffusion terms in the Navier-Stokes equations are discretised using a secondorder central difference scheme, and a low storage twostep Runge-Kutta method is used to advance simulations in time. Predicted velocities are corrected using a Poisson pressure equation with a multi-grid technique following a fully explicit fractional step method. The wall-adapting local-eddy viscosity (WALE) sub-grid scale model [20] is used to approximate the unresolved anisotropic flow scales in this study.

The Immersed Boundary Method (IBM) is used in DOFAS to efficiently represent the static geometries such ridges and turbine hub and tower. This discrete approach is based on the direct forcing method [21]. Velocities and forces are interpolated using the ϕ_3 delta function of Roma et al. [22] with three neighbours in each direction to reduce computational overhead. The Actuator Line Method (ALM) adopted in DOFAS divides turbine blades into lines of moving Lagrangian markers along the blade length based on grid resolution with the use of a tip-loss correction of Prandtl-type [23]. The interpolation process is performed using a non-isotropic Gaussian projection [24].

III. DESCRIPTION OF TEST CASES

The laboratory-scale tidal stream turbine from Stallard et al. [25] is considered in this work, as this was previously validated with DOFAS using the same

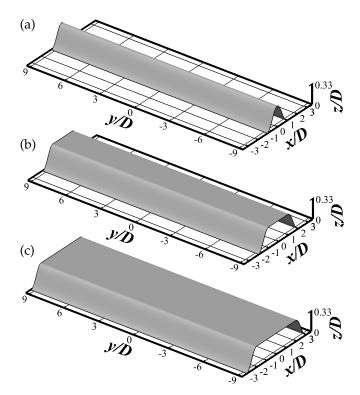


Fig. 1. Representation of the idealised ridge-type bathymetries used in cases with length of (a) 2DR, (b) 4DR and (c) 6DR.

experimental flow conditions [18], [19]. Herein, a flatbed simulation is run initially using a depth-averaged velocity (U_0) of 0.47 m·s⁻¹ that is distributed vertically following the smooth logarithmic distribution in the experiment with a channel depth of 0.45 m. The turbine has a diameter (D) of 0.27 m and the hub height is centred at the channel mid depth connected to a bottomfixed vertical tower. The turbine in this case operates at a rotational speed of 15.7 rad·s⁻¹, corresponding to an optimal Tip Speed Ratio (TSR) of 4.43. At this ratio, the resulted thrust and power coefficient are 0.84 and 0.3, respectively [25].

To compare the wake characteristics between flat and complex seabed bathymetry, three ridges with symmetric shapes are chosen as fundamental analysis on the impact of terrain complexity on tidal stream turbines. Fig. 1 show symmetric ridges with varying lengths used herein starting with 2D for the Gaussian-shape ridge shown in Fig. 1a. The ridge slope is characterised by the following equation:

$$Z(x) = \frac{1}{2}h\left[1 + \cos\left(\frac{\pi x}{l}\right)\right] \tag{1}$$

Here, h=H-1.67D represents the height of the ridge, and l is the horizontal length of the slope. The resulted mean slope angle is 27.62° , whereas the local maximum angle is 18.40° . By keeping constant ridge slope at the upstream and downstream sides, ridge length is elongated by applying a flat top reaching a total length of 4D and 6D for the other tested ridges as illustrated in Fig. 1. Ridge centre is located at 15D from the inlet in all cases. The same setup of the flatbed case is applied for ridge cases, whereas the channel depth is adjusted in case of a ridge to maintain similar

TABLE I

Disc-averaged of normalised mean velocity (U_D) , turbulence intensity (u_D') obtained in the flat-bed case and the three ridges at the simulated turbine positions. Last column shows the adopted rotational speed (Ω) based on the U_D value at each position such that the turbine develops the same tip speed ratio at each position.

Flat			
Position	U_D/U_0	u_D'/U_0	Ω
	-	%	$\mathrm{rad}\cdot\mathrm{s}^{-1}$
TF	1.01	7.56	15.7
Ridge case: 2DR			
T2U	1.02	7.44	15.7
T2C	1.19	7.45	18.9
T2D	1.16	12.76	17.8
Ridge case: 4DR			
T4U	1.02	7.60	15.7
T4C	1.23	7.55	19.1
T4D	1.11	12.42	17.4
Ridge case: $6DR$			
T6U	1.01	7.92	15.7
T6C	1.24	7.81	19.1
T6D	1.07	11.54	17.3

depth-to-diameter (H/D) ratio of 1.67D at the highest point of the ridge to the flat-bed case.

For each ridge, three turbine positions are selected. The first is located at a distance of 2D upstream of the ridge foot (labelled as "Turbine Upstream", TU), the second is at the ridge centre on the crest (referenced to as "Turbine Centre", TC), and a third position that is identical to the first one downstream of the ridge (labelled as "Turbine Downstream", TD). These positions are selected so that they account for the ebb and flood phases of a tidal cycle in which the tidal stream turbine would face the flow from two directions relative to the ridge position, e.g. in one tidal flow direction the ridge is downstream of the turbine and vice versa. The hub height is constant of 0.83D from the local bottom bathymetry.

In order to maintain the same tip speed ratio to that in the flat-bed case, the rotational speed is adjusted based on the disc-averaged velocity (U_D) calculated at the turbine position from the precursor simulations performed without turbines. The disc-averaged velocity U_D is computed over the rotor swept area as:

$$U_D = \frac{1}{A_D} \sum U(x, y, z) dy dz \tag{2}$$

where A_D is disc area and U(x,y,z) is the timeaveraged streamwise velocity at the cell whose dimensions are dy and dz in the lateral and vertical directions, respectively.

Table I shows the normalised disc-averaged velocity, turbulence intensity and the adopted rotational speed so that all turbine operate at their optimal tip speed ratio for the flat-bed and ridge cases.

The simulation domain has dimensions of 49D in the streamwise direction and 18.5D in the spanwise direction. However, in the vertical direction, the flatbed case has a depth of 1.67D, while the ridge cases

have a depth of 2*D*. Simulations are run for 225 s with a fixed time step of 0.001 s and a uniform grid resolution of 0.005 m that leads to a total of 237.6 and 285.12 million grid point in the flat and ridge cases, respectively. The time step and grid resolution used in this study have been previously demonstrated to yield accurate results for flow statistics and the hydrodynamic coefficients of the turbine used here [19].

The inflow velocity distribution, with a depthaveraged velocity of $U_0 = 0.47 \text{ m s}^{-1}$, is computed using a logarithmic distribution, as obtained in experiments [25], with a friction velocity (u_{\star}) equal to 0.0187 m s^{-1} . A Synthetic Eddy Method (SEM) is used to numerically superimpose artificial turbulence at the inlet with an intensity $I_x = 15\%$, which decreased further downstream to a nearly constant level of 7% along the channel, and turbulence length scales of 0.56H, 0.33Hand 0.25H in the streamwise, spanwise and wallnormal directions, respectively. A convective outflow boundary condition is set at the outlet, whereas the top surface is treated with a shear-free slip condition. The spanwise boundaries are set to periodic boundary conditions in order to decrease the lateral blockage if walls were used, and a smooth-bed wall function is used at the bottom surface as the grid resolution in wall units is approx. 55 [19].

IV. RESULTS

A. Flow over ridges

The mean velocity distribution in the ridge cases with no turbine is shown in Fig. 2. In all ridge cases, the flow accelerates over the upstream slope. This is due to the favorable pressure gradient induced by the ridge [5]. Over the ridge top, it is observed that the accelerated flow persist along the elongated flat surface when ridge length is increased. On the downstream side of the ridge, a recirculated region is developed with negative values of U/U_0 . The flow on the downstream side of the ridge exhibits the fundamental characteristics of a separated flow, which are similar to those observed in studies of separation flow at backward facing steps [26].

Fig. 3 present the vertical profiles of the mean velocity, turbulence intensity and vertical Reynolds shear stress at different downstream positions from ridge centre, with vertical coordinates normalised considering the origin (z/D=0) at hub height. As seen in Fig. 3, turbines to be deployed upstream of the ridges (TU) are subjected to a similar streamwise velocity distribution and to less than 2% difference in velocity fluctuations. However, the wake of these turbines would experience a flow acceleration once reaching the ridge top that will contribute to a faster wake recovery together with the high shear developed downstream of the ridge, observed in the increased levels of turbulence intensity and Reynolds shear stress in Fig. 2.

For turbine positions located at the centre of the ridge top (TC) at x/D=0, the vertical distribution of the streamwise velocity is approximately uniform

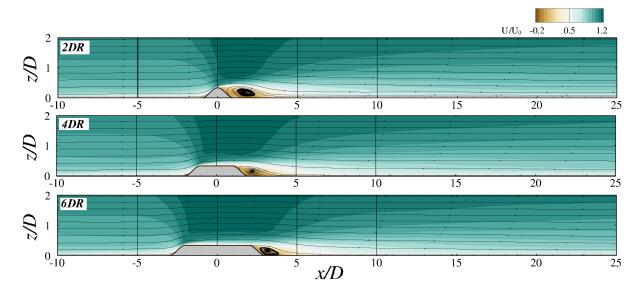


Fig. 2. Normalised mean streamwise velocity contours over xz-plane for the ridge cases going through the channel centre. The center of the ridge is used as a local coordinate reference in the x-axis.

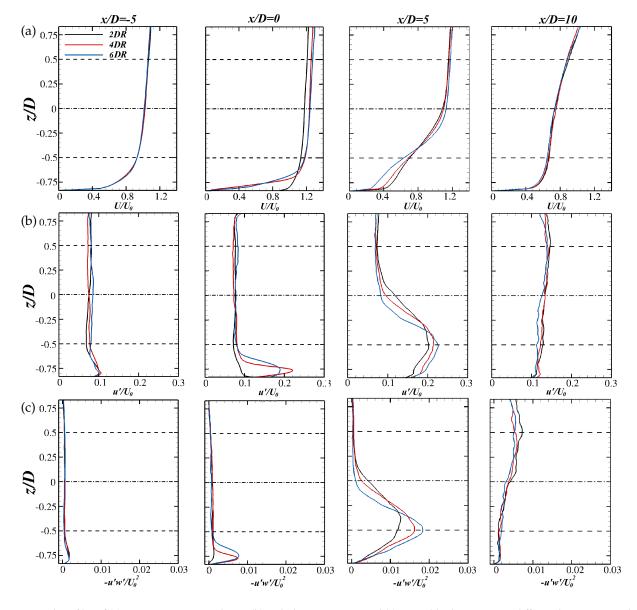


Fig. 3. Vertical profiles of (a) mean streamwise velocity, (b) turbulence intensity and (c) Reynolds shear stress at different locations as indicated with black lines in Fig. 1. Black dashed line shows the turbine area and turbine centre is used as a local coordinate reference in the z-axis.

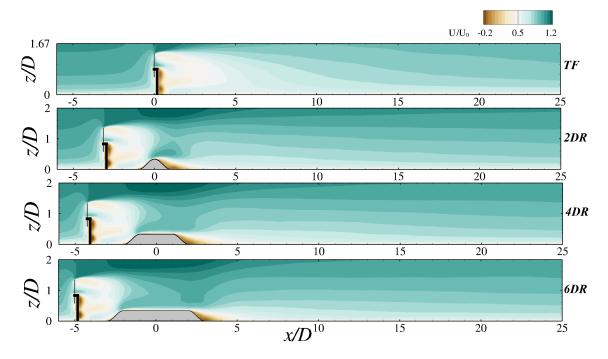


Fig. 4. Normalised mean streamwise velocity contours over xz-plane for the flat-bed case and upstream turbines (TU) in the ridge cases.

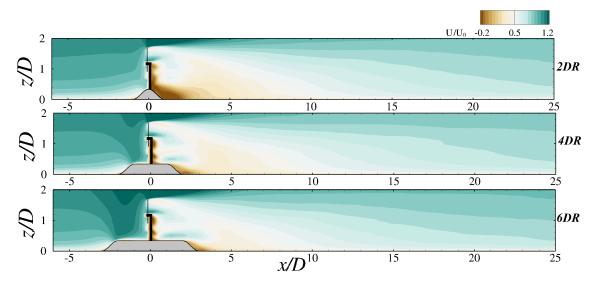


Fig. 5. Normalised mean streamwise velocity contours over xz-plane for the turbines located on ridge tops (TC).

across the water depth. At this location, the discaveraged velocity is increased by 19%, 23% and 24% from the undisturbed depth averaged velocity at the 2DR, 4DR and 6DR cases, respectively, as seen in Table I. At the same location, Fig. 3b shows an increase in turbulence intensity levels near the bottom for 4DR and 6DR cases over the ridge's flat surface. This increase is due to the high flow shear induced by the wake downstream of the crest of the ridge's leading edge which decreases as the flow continued downstream [27].

Turbines downstream of the ridge (TD) are expected to be subjected to a highly-sheared mean velocity profile that has lower values below the bottom tip of the turbine compared to the other locations. This flow shear is steeper for the 2DR case. Furthermore, Table I shows that the disc-averaged velocity and

turbulence intensity for TD turbines decrease as ridge length increases. This is due to the recirculation region in the lee side of the ridge, which causes high velocity fluctuations and intense turbulent momentum exchange due to the shear layer formed there. The effect of the recirculated region is more pronounced in the 2DR ridge case as the flow is deflected upwards over the lee side of the ridge. Whereas for the elongated ridges (4DR) and (4DR), the flow deflected from the upstream ridge slope is recovered over the flat surface on the ridge top and therefore the recirculating flow downstream of the ridge is reduced.

B. Wake deficit

The distribution of mean velocity in the presence of the turbine is shown in Fig. 4 for the flat-bed case and upstream turbines. For all of the considered

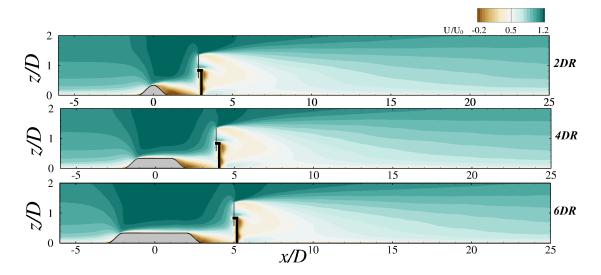


Fig. 6. Normalised mean streamwise velocity contours over xz-plane for the downstream turbines (TD).

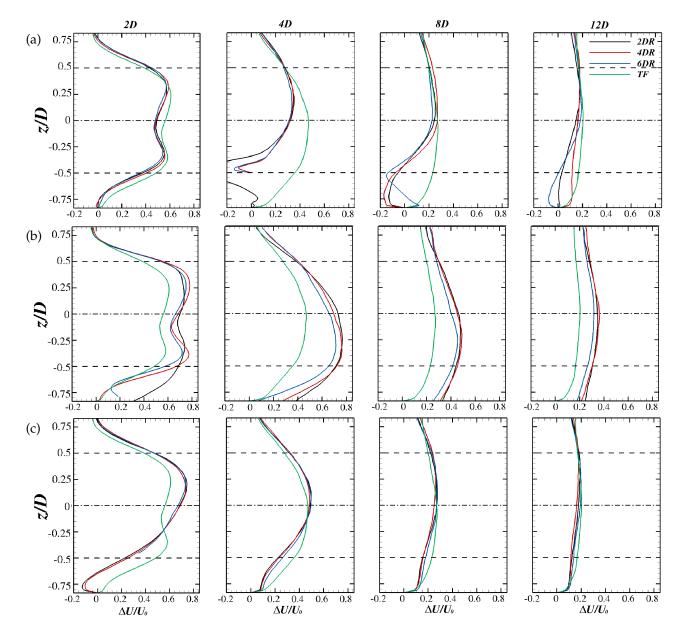


Fig. 7. Vertical distribution of velocity deficit at 2D, 4D, 8D and 12D downstream of the rotor for (a) upstream turbines and the flat-bed case, (b) turbines at ridge centre and (c) downstream turbines. Black dashed line shows the turbine area and turbine centre is used as a local coordinate reference in the z-axis.

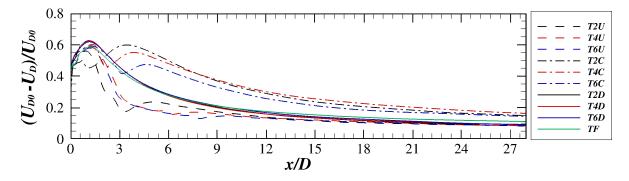


Fig. 8. Disc-averaged velocity deficit normalised by the disc-averaged velocity of the flow with no-turbine. Turbines are located at x/D=0.

ridge lengths, it can be seen that the slow wake flow generated by the turbine is reduced at the ridge leading edge due to the effect of the favorable pressure gradient. However, downstream of the ridge, turbine wakes merge with ridge wake which contribute to the over all flow reduction there.

To analyse this further, vertical profiles of velocity deficit ($\triangle U$) at 2D, 4D, 8D and 12D downstream of the rotor are presented in Fig. 7. The deficit is calculated by removing the flow field from the simulation with no turbine from that in which a turbine is simulated, in order to isolate the ridge wake from turbine wake. Thus the velocity deficit is computed as $\triangle U(x, y, z) = U_{NT}(x, y, z) - U_{T}(x, y, z)$, where U_{NT} and U_T denote the mean streamwise velocity in the absence and presence of a turbine, respectively. Fig. 7a shows the vertical distribution of velocity deficit for the flat-bed and TU cases. It can be seen that at 4D, the deficit is reduced by approximately 75% from the depth-averaged velocity, whereas this reduction is achieved at approximately 8D for the flat-bed case. A negative deficit is observed in the lower half of the wake for the ridge cases, which indicates that the flow in the presence of the turbine is faster than the flow over the ridge alone. This is due to the bypass flow around the turbine, which is deflected upwards over the ridge region.

Fig. 5 shows the mean velocity distribution for turbines sited at the ridge top. At this location, turbine wakes are likely to extend for a long distance downstream of the turbine due to the adverse pressure gradient generated in the lee side of the ridge. Vertical profiles for TC turbines (see Fig. 7b) show that the wake persists for a longer distance compared to turbine wakes in the other locations or in the flat-bed case. At a distance of 12D, approximately 35% of velocity deficit is reached for TC cases compared to 20% for TD turbines, as seen in Fig. 7. It is noteworthy that in the case of 6DR, the observed wake deficit is slightly lower than in the case of 4DR and 2DR. This could be attributed to the longer distance between the turbine and the adverse pressure side of the ridge.

For the downstream turbines shown in Fig. 6, velocity distribution downstream of the turbine show similar distribution for all ridge lengths, again seen in Fig. 7c with almost identical profiles of velocity deficit. However, comparing to the flat-bed case, wake

recovery for TD turbines is similar to the flat-bed case beyond 8D although this location is subjected to higher turbulence intensity comparing to the flat-bed and a faster wake recovery is expected. This observation could be attributed to that turbines in this location operate in the accelerated flow induced by ridge presence (see Fig. 6), therefore, their wake is under adverse pressure gradient.

To analyse wake recovery with downstream distance, Fig. 8 shows the disc-averaged velocity deficit evolution along the downstream direction normalised by the disc-averaged velocity with no turbine. For the flat-bed case, the velocity deficit remains approximately 15% at 15.4D downstream of the turbine, i.e. 85% wake recovery. A similar velocity deficit is found at downstream distances of 10.9D, 10D, and 6.8D for TU locations in the 2DR, 4DR, and 6DR cases respectively, whereas for TC locations, a 15% velocity deficit threshold is achieved further downstream at a distances beyond 25D compared to the flat-bed case. Considering turbines downstream of the ridge, similar to the observations in Fig. 7, TD locations show a similar trend in wake recovery to the flat-bed case; however, 15% of velocity deficit is attained closer to the turbine by 1.7D in the case of 6DR, and by 2.6Din the case of 4DR and 2DR when compared to the flat-bed case.

C. Fatigue loads

Fatigue loads acting on the turbine structure are determined using Damage Equivalent Loads (DELs) [28]. A rainflow cycle counting method [29] is used to identify the range of load cycles experienced by the turbine blades over the operation time. The time history of the forces computed with the ALM are analysed and the DELs are calculated using the number of load cycles and the load range over the simulated turbine revolutions following the formula:

$$DEL = \left(\frac{\sum_{i} n_{i} F_{i}^{m}}{N}\right)^{\frac{1}{m}} \tag{3}$$

where for every bin i, the variables n_i and F_i represent the number of load cycles and load range, respectively, m is the material property, and N is the turbine rotations.

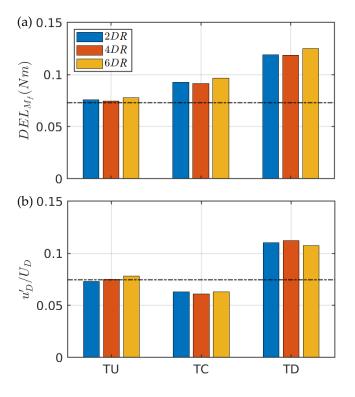


Fig. 9. Comparison of three ridges of (a) Damage Equivalent Loads (DELs) of flapwise bending moment acting on a single blade and (b) disc-averaged turbulence intensity normalised by the disc-averaged mean velocity for the tested cases with the black dashed-dotted line shows the values for the flat-bed case.

Fig. 9 illustrates the DELs of the flapwise bending moment M_f acting on a single blade and the discaveraged turbulence intensity normalised by the discaveraged mean velocity. The DELs for the upstream turbines are similar to that for the flat-bed case (shown in black dashed-dotted line), as the flow conditions in these areas are comparable. However, the DELs for turbines located on ridge tops (TC turbines) show a slight increase, which can be attributed to the high mean load value resulting from the accelerated flow. Despite this increase, the velocity fluctuations at these locations are approximately similar to those for upstream turbines (see Table I). In contrast, downstream turbines exhibit the highest DELs, due to both the high load values and fluctuations present in these areas.

V. CONCLUSION

In this study, the influence of symmetric ridges on the wake and loading of a single tidal stream turbine is assessed through large-eddy simulations of a laboratory-scale turbine located at different positions relative to three different ridge lengths. The results show that, turbine wake recovers more rapidly when the turbine is located a short distance upstream of a symmetric ridge, with the distance to a deficit recovery of 15% reduced to 10.9D in the short ridge length, approximately 29% shorter than for the wake of the same turbine over a flat-bed. This distance reduces further for increased ridge length up to about 55% smaller than the flat-bed in case for the long ridge length. For turbines located on ridge tops, much longer wakes are observed compared to other locations, with

a slight decrease of recovery distance for longer ridges. Considering downstream turbines, the wake recovery is very similar to that found in turbines operating over a flat surface.

Analysis of fatigue loads acting on rotor blades indicate that turbines located on ridge top experience high mean load values due to be deployed in a region of flow acceleration, whilst turbines downstream of a ridge are subjected to greater fatigue loads due to operation in region with elevated levels of turbulence. Considering a full tidal cycle with the assumption that the flow statistics are similar in both directions, TU and TD would represent the same turbine in this cycle and the aggregated damage equivalent loads could be higher in this location comparing to the one at the ridge top. These results outline the need for detailed analyses of relative turbine locations in proximity to bathymetric features such as ridges.

These findings suggest that for a multi-rows tidal stream array, a ridge presence between rows could have a positive impact in terms of wake recovery rate as the downstream turbines would be less affected by the upstream turbine wake. Conversely, fatigue loads for turbines downstream of a ridge are increased due to ridge induced turbulence. Further analysis is required for tidal turbine arrays to quantify fatigue loads on secondary row turbines in both ridge presence and absence.

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